

國立屏東教育大學 99 學年度研究所碩士班入學考試

統計學 試題

(應用數學系碩士班)

※請注意：1.本試題共六頁，附統計表 A、B、C、D 等共四頁。

2.答案須寫在答案卷上，否則不予計分。

問答題 (共 100 分)

一、請寫出簡單線性迴歸的模型與假設。(10 分)

二、某國即將總統大選，因此想了解兩位總統候選人的選民支持度，在兩個城市各隨機電訪 500 位選民，詢問其對兩位總統候選人的支持情形，資料如下：

| 選民支持情形 | 城市 | |
|----------|----------|---------|
| | Richmond | Norfolk |
| 支持 A 候選人 | 204 | 225 |
| 支持 B 候選人 | 211 | 198 |
| 尚未決定 | 85 | 77 |

在顯著水準 0.05 之下檢定虛無假設，虛無假設是在這兩個城市支持 A 候選人、支持 B 候選人與尚未決定等三者的比例相同。(20 分)

三、某學者想了解市售 3 大品牌花生醬的食鹽含量，從市場上隨機抽取 3 大品牌花生醬各 6 罐檢測其食鹽含量，運用統計軟體分析資料，(1) 請寫出此統計分析的統計模型與假設；(2) 請完成下列表格；(3) 在顯著水準 0.05 之下，是否市售 3 大品牌花生醬的平均食鹽含量有顯著的差異？(20 分)

Analysis of Variance

| Source | SS | DF | MS | F |
|--------|-------|----|----|---|
| Group | | | | |
| Error | 54.88 | | | |
| Total | 59.56 | | | |

四、某政府單位想知道 A 市與 B 市家庭平均收入的差異，已知兩母體變異數大約相等，抽查的結果如下：

| | 樣本數 | 平均收入 | 標準差 |
|-----|-----|---------|--------|
| A 市 | 35 | 401,800 | 20,000 |
| B 市 | 40 | 388,000 | 22,000 |

(1) 在顯著水準為 0.05 時，檢定兩市之家庭平均收入有無差異？(15 分)

(2) 試求 p-value。(5 分)

五、某地區發生六級以上地震的次數為平均每 10 年 2 次的卜瓦松分配，試求今年發生六級以上地震的機率？(10 分)

六、有一製造包裝鮮奶盒子之生產線，盒子重量訂為 150 公克，由於生產過程中的誤差，盒子之平均重量，會有高於或低於 150 公克現象，今品管員抽出 6 個樣本，資料如下：

155 146 144 152 158 153

當樣本資料顯示平均重量不等於 150 公克時(顯著水準 $\alpha=0.05$)，則生產線必需停工調整。

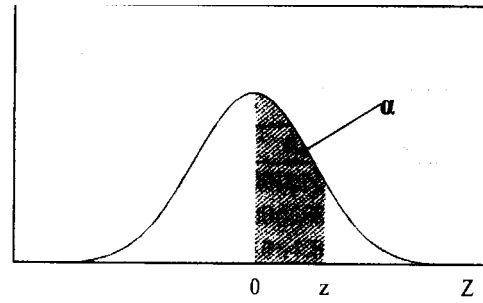
(1) 若盒子的重量是常態分配，問生產線要停工調整嗎？(10 分)

(2) 檢定盒子重量的變異數 σ^2 是否等於 25？(10 分)

統計表 A

表三 標準常態累加機率值表

$$P(0 < Z < z) = \alpha$$

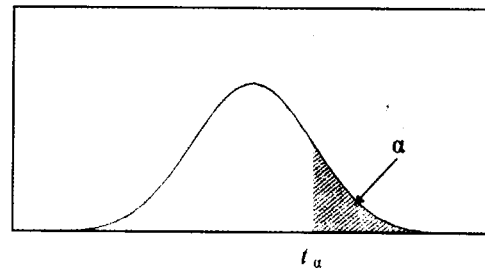


| <i>z</i> | .00 | .01 | .02 | .03 | .04 | .05 | .06 | .07 | .08 | .09 |
|----------|------------|---------|---------|---------|---------|---------|---------|---------|---------|---------|
| 0.0 | 0.0000 | 0.0040 | 0.0080 | 0.0120 | 0.0160 | 0.0199 | 0.0239 | 0.0279 | 0.0319 | 0.0359 |
| 0.1 | 0.0398 | 0.0438 | 0.0478 | 0.0517 | 0.0557 | 0.0596 | 0.0636 | 0.0675 | 0.0714 | 0.0753 |
| 0.2 | 0.0793 | 0.0832 | 0.0871 | 0.0910 | 0.0948 | 0.0987 | 0.1026 | 0.1064 | 0.1103 | 0.1141 |
| 0.3 | 0.1179 | 0.1217 | 0.1255 | 0.1293 | 0.1331 | 0.1368 | 0.1406 | 0.1443 | 0.1480 | 0.1517 |
| 0.4 | 0.1554 | 0.1591 | 0.1628 | 0.1664 | 0.1700 | 0.1736 | 0.1772 | 0.1808 | 0.1844 | 0.1879 |
| 0.5 | 0.1915 | 0.1950 | 0.1985 | 0.2019 | 0.2054 | 0.2088 | 0.2123 | 0.2157 | 0.2190 | 0.2224 |
| 0.6 | 0.2257 | 0.2291 | 0.2324 | 0.2357 | 0.2389 | 0.2422 | 0.2454 | 0.2486 | 0.2517 | 0.2549 |
| 0.7 | 0.2580 | 0.2611 | 0.2642 | 0.2673 | 0.2704 | 0.2734 | 0.2764 | 0.2794 | 0.2823 | 0.2852 |
| 0.8 | 0.2881 | 0.2910 | 0.2939 | 0.2967 | 0.2995 | 0.3023 | 0.3051 | 0.3078 | 0.3106 | 0.3133 |
| 0.9 | 0.3159 | 0.3186 | 0.3212 | 0.3238 | 0.3264 | 0.3289 | 0.3315 | 0.3340 | 0.3365 | 0.3389 |
| 1.0 | 0.3413 | 0.3438 | 0.3461 | 0.3485 | 0.3508 | 0.3531 | 0.3554 | 0.3577 | 0.3599 | 0.3621 |
| 1.1 | 0.3643 | 0.3665 | 0.3686 | 0.3708 | 0.3729 | 0.3749 | 0.3770 | 0.3790 | 0.3810 | 0.3830 |
| 1.2 | 0.3849 | 0.3869 | 0.3888 | 0.3907 | 0.3925 | 0.3944 | 0.3962 | 0.3980 | 0.3997 | 0.4015 |
| 1.3 | 0.4032 | 0.4049 | 0.4066 | 0.4082 | 0.4099 | 0.4115 | 0.4131 | 0.4147 | 0.4162 | 0.4177 |
| 1.4 | 0.4192 | 0.4207 | 0.4222 | 0.4236 | 0.4251 | 0.4265 | 0.4279 | 0.4292 | 0.4306 | 0.4319 |
| 1.5 | 0.4332 | 0.4345 | 0.4357 | 0.4370 | 0.4382 | 0.4394 | 0.4406 | 0.4418 | 0.4429 | 0.4441 |
| 1.6 | 0.4452 | 0.4463 | 0.4474 | 0.4484 | 0.4495 | 0.4505 | 0.4515 | 0.4525 | 0.4535 | 0.4545 |
| 1.7 | 0.4554 | 0.4564 | 0.4573 | 0.4582 | 0.4591 | 0.4599 | 0.4608 | 0.4616 | 0.4625 | 0.4633 |
| 1.8 | 0.4641 | 0.4649 | 0.4656 | 0.4664 | 0.4671 | 0.4678 | 0.4686 | 0.4693 | 0.4699 | 0.4706 |
| 1.9 | 0.4713 | 0.4719 | 0.4726 | 0.4732 | 0.4738 | 0.4744 | 0.4750 | 0.4756 | 0.4761 | 0.4767 |
| 2.0 | 0.4772 | 0.4778 | 0.4783 | 0.4788 | 0.4793 | 0.4798 | 0.4803 | 0.4808 | 0.4812 | 0.4817 |
| 2.1 | 0.4821 | 0.4826 | 0.4830 | 0.4834 | 0.4838 | 0.4842 | 0.4846 | 0.4850 | 0.4854 | 0.4857 |
| 2.2 | 0.4861 | 0.4864 | 0.4868 | 0.4871 | 0.4875 | 0.4878 | 0.4881 | 0.4884 | 0.4887 | 0.4890 |
| 2.3 | 0.4893 | 0.4896 | 0.4898 | 0.4901 | 0.4904 | 0.4906 | 0.4909 | 0.4911 | 0.4913 | 0.4916 |
| 2.4 | 0.4918 | 0.4920 | 0.4922 | 0.4925 | 0.4927 | 0.4929 | 0.4931 | 0.4932 | 0.4934 | 0.4936 |
| 2.5 | 0.4938 | 0.4940 | 0.4941 | 0.4943 | 0.4945 | 0.4946 | 0.4948 | 0.4949 | 0.4951 | 0.4952 |
| 2.6 | 0.4953 | 0.4955 | 0.4956 | 0.4957 | 0.4959 | 0.4960 | 0.4961 | 0.4962 | 0.4963 | 0.4964 |
| 2.7 | 0.4965 | 0.4966 | 0.4967 | 0.4968 | 0.4969 | 0.4970 | 0.4971 | 0.4972 | 0.4973 | 0.4974 |
| 2.8 | 0.4974 | 0.4975 | 0.4976 | 0.4977 | 0.4977 | 0.4978 | 0.4979 | 0.4979 | 0.4980 | 0.4981 |
| 2.9 | 0.4981 | 0.4982 | 0.4982 | 0.4983 | 0.4984 | 0.4984 | 0.4985 | 0.4985 | 0.4986 | 0.4986 |
| 3.0 | 0.49865 | 0.49869 | 0.49874 | 0.49878 | 0.49882 | 0.49886 | 0.49889 | 0.49893 | 0.49897 | 0.49900 |
| 3.1 | 0.49903 | 0.49906 | 0.49910 | 0.49913 | 0.49916 | 0.49918 | 0.49921 | 0.49924 | 0.49926 | 0.49929 |
| 3.2 | 0.49931 | 0.49934 | 0.49936 | 0.49938 | 0.49940 | 0.49942 | 0.49944 | 0.49946 | 0.49948 | 0.49950 |
| 3.3 | 0.49952 | 0.49953 | 0.49955 | 0.49967 | 0.49958 | 0.49960 | 0.49961 | 0.49962 | 0.49964 | 0.49965 |
| 3.4 | 0.49966 | 0.49968 | 0.49969 | 0.49970 | 0.49971 | 0.49972 | 0.49973 | 0.49974 | 0.49975 | 0.49976 |
| 3.5 | 0.49977 | 0.49978 | 0.49978 | 0.49979 | 0.49980 | 0.49981 | 0.49981 | 0.49982 | 0.49983 | 0.49983 |
| 3.6 | 0.49984 | 0.49985 | 0.49985 | 0.49986 | 0.49986 | 0.49987 | 0.49987 | 0.49988 | 0.49988 | 0.49989 |
| 3.7 | 0.49989 | 0.49990 | 0.49990 | 0.49990 | 0.49991 | 0.49991 | 0.49992 | 0.49992 | 0.49992 | 0.49992 |
| 3.8 | 0.49993 | 0.49993 | 0.49993 | 0.49994 | 0.49994 | 0.49994 | 0.49994 | 0.49995 | 0.49995 | 0.49995 |
| 3.9 | 0.49995 | 0.49995 | 0.49996 | 0.49996 | 0.49996 | 0.49996 | 0.49996 | 0.49996 | 0.49997 | 0.49997 |
| 4.0 | 0.49996832 | | | | | | | | | |
| 4.5 | 0.49999660 | | | | | | | | | |
| 5.0 | 0.49999971 | | | | | | | | | |
| 5.5 | 0.49999998 | | | | | | | | | |
| 6.0 | 0.49999999 | | | | | | | | | |

統計表 B

表五 t 分配臨界值表

$$P(t > t_{\alpha}) = \alpha$$

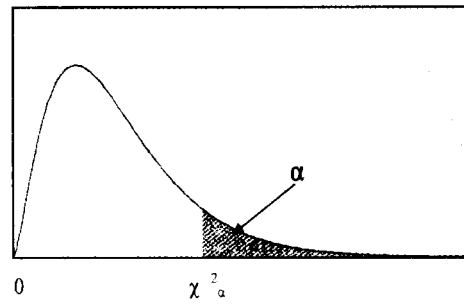


| <i>d.f.</i> | $t_{.100}$ | $t_{.050}$ | $t_{.025}$ | $t_{.010}$ | $t_{.005}$ | <i>d.f.</i> |
|-------------|------------|------------|------------|------------|------------|-------------|
| 1 | 3.078 | 6.314 | 12.706 | 31.821 | 63.656 | 1 |
| 2 | 1.886 | 2.920 | 4.303 | 6.965 | 9.925 | 2 |
| 3 | 1.638 | 2.353 | 3.182 | 4.541 | 5.841 | 3 |
| 4 | 1.533 | 2.132 | 2.776 | 3.747 | 4.604 | 4 |
| 5 | 1.476 | 2.015 | 2.571 | 3.365 | 4.032 | 5 |
| 6 | 1.440 | 1.943 | 2.447 | 3.143 | 3.707 | 6 |
| 7 | 1.415 | 1.895 | 2.365 | 2.998 | 3.499 | 7 |
| 8 | 1.397 | 1.860 | 2.306 | 2.896 | 3.355 | 8 |
| 9 | 1.383 | 1.833 | 2.262 | 2.821 | 3.250 | 9 |
| 10 | 1.372 | 1.812 | 2.228 | 2.764 | 3.169 | 10 |
| 11 | 1.363 | 1.796 | 2.201 | 2.718 | 3.106 | 11 |
| 12 | 1.356 | 1.782 | 2.179 | 2.681 | 3.055 | 12 |
| 13 | 1.350 | 1.771 | 2.160 | 2.650 | 3.012 | 13 |
| 14 | 1.345 | 1.761 | 2.145 | 2.624 | 2.977 | 14 |
| 15 | 1.341 | 1.753 | 2.131 | 2.602 | 2.947 | 15 |
| 16 | 1.337 | 1.746 | 2.120 | 2.583 | 2.921 | 16 |
| 17 | 1.333 | 1.740 | 2.110 | 2.567 | 2.898 | 17 |
| 18 | 1.330 | 1.734 | 2.101 | 2.552 | 2.878 | 18 |
| 19 | 1.328 | 1.729 | 2.093 | 2.539 | 2.861 | 19 |
| 20 | 1.325 | 1.725 | 2.086 | 2.528 | 2.845 | 20 |
| 21 | 1.323 | 1.721 | 2.080 | 2.518 | 2.831 | 21 |
| 22 | 1.321 | 1.717 | 2.074 | 2.508 | 2.819 | 22 |
| 23 | 1.319 | 1.714 | 2.069 | 2.500 | 2.807 | 23 |
| 24 | 1.318 | 1.711 | 2.064 | 2.492 | 2.797 | 24 |
| 25 | 1.316 | 1.708 | 2.060 | 2.485 | 2.787 | 25 |
| 26 | 1.315 | 1.706 | 2.056 | 2.479 | 2.779 | 26 |
| 27 | 1.314 | 1.703 | 2.052 | 2.473 | 2.771 | 27 |
| 28 | 1.313 | 1.701 | 2.048 | 2.467 | 2.763 | 28 |
| 29 | 1.311 | 1.699 | 2.045 | 2.462 | 2.756 | 29 |
| 30 | 1.310 | 1.697 | 2.042 | 2.457 | 2.750 | 30 |
| 31 | 1.310 | 1.696 | 2.040 | 2.453 | 2.744 | 31 |
| 32 | 1.309 | 1.694 | 2.037 | 2.449 | 2.739 | 32 |
| 33 | 1.308 | 1.692 | 2.035 | 2.445 | 2.733 | 33 |
| 34 | 1.307 | 1.691 | 2.032 | 2.441 | 2.728 | 34 |
| 35 | 1.306 | 1.690 | 2.030 | 2.438 | 2.724 | 35 |
| 36 | 1.306 | 1.688 | 2.028 | 2.435 | 2.720 | 36 |
| 37 | 1.305 | 1.687 | 2.026 | 2.431 | 2.715 | 37 |
| 38 | 1.304 | 1.686 | 2.024 | 2.429 | 2.712 | 38 |
| 39 | 1.304 | 1.685 | 2.023 | 2.426 | 2.708 | 39 |
| 40 | 1.303 | 1.684 | 2.021 | 2.423 | 2.705 | 40 |
| ∞ | 1.282 | 1.645 | 1.960 | 2.326 | 2.576 | ∞ |

統計表 C

表六 卡方分配臨界值表 (續)

$$P(\chi^2 > \chi^2_{\alpha}) = \alpha$$

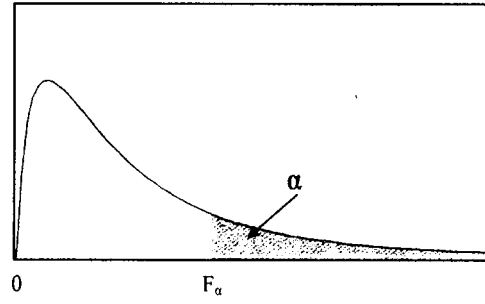


| $\chi^2_{0.100}$ | $\chi^2_{0.050}$ | $\chi^2_{0.025}$ | $\chi^2_{0.010}$ | $\chi^2_{0.005}$ | <i>d.f.</i> |
|------------------|------------------|------------------|------------------|------------------|-------------|
| 2.705541 | 3.841455 | 5.023903 | 6.634891 | 7.879400 | 1 |
| 4.605176 | 5.991476 | 7.377779 | 9.210351 | 10.5965 | 2 |
| 6.251394 | 7.814725 | 9.348404 | 11.3449 | 12.8381 | 3 |
| 7.779434 | 9.487728 | 11.1433 | 13.2767 | 14.8602 | 4 |
| 9.236349 | 11.0705 | 12.8325 | 15.0863 | 16.7496 | 5 |
| 10.6446 | 12.5916 | 14.4494 | 16.8119 | 18.5475 | 6 |
| 12.0170 | 14.0671 | 16.0128 | 18.4753 | 20.2777 | 7 |
| 13.3616 | 15.5073 | 17.5345 | 20.0902 | 21.9549 | 8 |
| 14.6837 | 16.9190 | 19.0228 | 21.6660 | 23.5893 | 9 |
| 15.9872 | 18.3070 | 20.4832 | 23.2093 | 25.1881 | 10 |
| 17.2750 | 19.6752 | 21.9200 | 24.7250 | 26.7569 | 11 |
| 18.5493 | 21.0261 | 23.3367 | 26.2170 | 28.2997 | 12 |
| 19.8119 | 22.3620 | 24.7356 | 27.6882 | 29.8193 | 13 |
| 21.0641 | 23.6848 | 26.1189 | 29.1412 | 31.3194 | 14 |
| 22.3071 | 24.9958 | 27.4884 | 30.5780 | 32.8015 | 15 |
| 23.5418 | 26.2962 | 28.8453 | 31.9999 | 34.2671 | 16 |
| 24.7690 | 27.5871 | 30.1910 | 33.4087 | 35.7184 | 17 |
| 25.9894 | 28.8693 | 31.5264 | 34.8052 | 37.1564 | 18 |
| 27.2036 | 30.1435 | 32.8523 | 36.1908 | 38.5821 | 19 |
| 28.4120 | 31.4104 | 34.1696 | 37.5663 | 39.9969 | 20 |
| 29.6151 | 32.6706 | 35.4789 | 38.9322 | 41.4009 | 21 |
| 30.8133 | 33.9245 | 36.7807 | 40.2894 | 42.7957 | 22 |
| 32.0069 | 35.1725 | 38.0756 | 41.6383 | 44.1814 | 23 |
| 33.1962 | 36.4150 | 39.3641 | 42.9798 | 45.5584 | 24 |
| 34.3816 | 37.6525 | 40.6465 | 44.3140 | 46.9280 | 25 |
| 35.5632 | 38.8851 | 41.9231 | 45.6416 | 48.2898 | 26 |
| 36.7412 | 40.1133 | 43.1945 | 46.9628 | 49.6450 | 27 |
| 37.9159 | 41.3372 | 44.4608 | 48.2782 | 50.9936 | 28 |
| 39.0875 | 42.5569 | 45.7223 | 49.5878 | 52.3355 | 29 |
| 40.2560 | 43.7730 | 46.9792 | 50.8922 | 53.6719 | 30 |
| 51.8050 | 55.7585 | 59.3417 | 63.6908 | 66.7660 | 40 |
| 63.1671 | 67.5048 | 71.4202 | 76.1538 | 79.4898 | 50 |
| 74.3970 | 79.0820 | 83.2977 | 88.3794 | 91.9518 | 60 |
| 96.5782 | 101.879 | 106.629 | 112.329 | 116.321 | 80 |
| 118.498 | 124.342 | 129.561 | 135.807 | 140.170 | 100 |

統計表 D

表八 F 分配臨界值表
(續)

$$P(F > F_\alpha) = \alpha$$



| $\nu_2(df)$ | $\nu_1(df)$ | | | | | | | | |
|-------------|-----------------|--------|--------|--------|--------|--------|--------|--------|--------|
| | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
| | $\alpha = 0.05$ | | | | | | | | |
| 1 | 161.45 | 199.50 | 215.71 | 224.58 | 230.16 | 233.99 | 236.77 | 238.88 | 240.54 |
| 2 | 18.51 | 19.00 | 19.16 | 19.25 | 19.30 | 19.33 | 19.35 | 19.37 | 19.38 |
| 3 | 10.13 | 9.55 | 9.28 | 9.12 | 9.01 | 8.94 | 8.89 | 8.85 | 8.81 |
| 4 | 7.71 | 6.94 | 6.59 | 6.39 | 6.26 | 6.16 | 6.09 | 6.04 | 6.00 |
| 5 | 6.61 | 5.79 | 5.41 | 5.19 | 5.05 | 4.95 | 4.88 | 4.82 | 4.77 |
| 6 | 5.99 | 5.14 | 4.76 | 4.53 | 4.39 | 4.28 | 4.21 | 4.15 | 4.10 |
| 7 | 5.59 | 4.74 | 4.35 | 4.12 | 3.97 | 3.87 | 3.79 | 3.73 | 3.68 |
| 8 | 5.32 | 4.46 | 4.07 | 3.84 | 3.69 | 3.58 | 3.50 | 3.44 | 3.39 |
| 9 | 5.12 | 4.26 | 3.86 | 3.63 | 3.48 | 3.37 | 3.29 | 3.23 | 3.18 |
| 10 | 4.96 | 4.10 | 3.71 | 3.48 | 3.33 | 3.22 | 3.14 | 3.07 | 3.02 |
| 11 | 4.84 | 3.98 | 3.59 | 3.36 | 3.20 | 3.09 | 3.01 | 2.95 | 2.90 |
| 12 | 4.75 | 3.89 | 3.49 | 3.26 | 3.11 | 3.00 | 2.91 | 2.85 | 2.80 |
| 13 | 4.67 | 3.81 | 3.41 | 3.18 | 3.03 | 2.92 | 2.83 | 2.77 | 2.71 |
| 14 | 4.60 | 3.74 | 3.34 | 3.11 | 2.96 | 2.85 | 2.76 | 2.70 | 2.65 |
| 15 | 4.54 | 3.68 | 3.29 | 3.06 | 2.90 | 2.79 | 2.71 | 2.64 | 2.59 |
| 16 | 4.49 | 3.63 | 3.24 | 3.01 | 2.85 | 2.74 | 2.66 | 2.59 | 2.54 |
| 17 | 4.45 | 3.59 | 3.20 | 2.96 | 2.81 | 2.70 | 2.61 | 2.55 | 2.49 |
| 18 | 4.41 | 3.55 | 3.16 | 2.93 | 2.77 | 2.66 | 2.58 | 2.51 | 2.46 |
| 19 | 4.38 | 3.52 | 3.13 | 2.90 | 2.74 | 2.63 | 2.54 | 2.48 | 2.42 |
| 20 | 4.35 | 3.49 | 3.10 | 2.87 | 2.71 | 2.60 | 2.51 | 2.45 | 2.39 |
| 21 | 4.32 | 3.47 | 3.07 | 2.84 | 2.68 | 2.57 | 2.49 | 2.42 | 2.37 |
| 22 | 4.30 | 3.44 | 3.05 | 2.82 | 2.66 | 2.55 | 2.46 | 2.40 | 2.34 |
| 23 | 4.28 | 3.42 | 3.03 | 2.80 | 2.64 | 2.53 | 2.44 | 2.37 | 2.32 |
| 24 | 4.26 | 3.40 | 3.01 | 2.78 | 2.62 | 2.51 | 2.42 | 2.36 | 2.30 |
| 25 | 4.24 | 3.39 | 2.99 | 2.76 | 2.60 | 2.49 | 2.40 | 2.34 | 2.28 |
| 26 | 4.23 | 3.37 | 2.98 | 2.74 | 2.59 | 2.47 | 2.39 | 2.32 | 2.27 |
| 27 | 4.21 | 3.35 | 2.96 | 2.73 | 2.57 | 2.46 | 2.37 | 2.31 | 2.25 |
| 28 | 4.20 | 3.34 | 2.95 | 2.71 | 2.56 | 2.45 | 2.36 | 2.29 | 2.24 |
| 29 | 4.18 | 3.33 | 2.93 | 2.70 | 2.55 | 2.43 | 2.35 | 2.28 | 2.22 |
| 30 | 4.17 | 3.32 | 2.92 | 2.69 | 2.53 | 2.42 | 2.33 | 2.27 | 2.21 |
| 40 | 4.08 | 3.23 | 2.84 | 2.61 | 2.45 | 2.34 | 2.25 | 2.18 | 2.12 |
| 60 | 4.00 | 3.15 | 2.76 | 2.53 | 2.37 | 2.25 | 2.17 | 2.10 | 2.04 |
| 120 | 3.92 | 3.07 | 2.68 | 2.45 | 2.29 | 2.18 | 2.09 | 2.02 | 1.96 |
| ∞ | 3.84 | 3.00 | 2.60 | 2.37 | 2.21 | 2.10 | 2.01 | 1.94 | 1.88 |